

Name: Key

Block: \_\_\_\_\_

Date: \_\_\_\_\_

### Cubes and Cube Roots

1. Without a calculator, find:

|                       |                     |                    |                     |
|-----------------------|---------------------|--------------------|---------------------|
| a. $7^3$<br><br>343   | b. $1^3$<br><br>1   | c. $4^3$<br><br>64 | d. $3^3$<br><br>27  |
| e. $10^3$<br><br>1000 | f. $5^3$<br><br>125 | g. $2^3$<br><br>8  | h. $6^3$<br><br>216 |

2. Use prime factorization to determine the following cube roots.

|  |  |
|--|--|
| <p>a. <math>\sqrt[3]{512}</math></p> $\begin{array}{r} 2 \overline{) 512} \\ \underline{256} \phantom{0} \\ 2 \overline{) 128} \\ \underline{64} \phantom{0} \\ 2 \overline{) 32} \\ \underline{16} \phantom{0} \\ 2 \overline{) 8} \\ \underline{4} \phantom{0} \\ 2 \overline{) 2} \\ \underline{2} \\ 0 \end{array}$ <p><math>\sqrt[3]{512} = \sqrt[3]{8 \cdot 8 \cdot 8}</math><br/><math>= \boxed{8}</math></p>           | <p>b. <math>\sqrt[3]{729}</math></p> $\begin{array}{r} 3 \overline{) 729} \\ \underline{243} \phantom{0} \\ 3 \overline{) 81} \\ \underline{27} \phantom{0} \\ 3 \overline{) 9} \\ \underline{3} \\ 0 \end{array}$ <p><math>\sqrt[3]{729} = \sqrt[3]{9 \cdot 9 \cdot 9}</math><br/><math>= \boxed{9}</math></p>  |
| <p>c. <math>\sqrt[3]{1728}</math></p> $\begin{array}{r} 2 \overline{) 1728} \\ \underline{864} \phantom{0} \\ 2 \overline{) 432} \\ \underline{216} \phantom{0} \\ 2 \overline{) 108} \\ \underline{54} \phantom{0} \\ 3 \overline{) 27} \\ \underline{9} \phantom{0} \\ 3 \overline{) 9} \\ \underline{3} \\ 0 \end{array}$ <p><math>\sqrt[3]{1728} = \sqrt[3]{12 \cdot 12 \cdot 12}</math><br/><math>= \boxed{12}</math></p> | <p>d. <math>\sqrt[3]{2744}</math></p> $\begin{array}{r} 2 \overline{) 2744} \\ \underline{1372} \phantom{0} \\ 2 \overline{) 686} \\ \underline{343} \phantom{0} \\ 7 \overline{) 49} \\ \underline{7} \\ 0 \end{array}$ <p><math>\sqrt[3]{2744} = \sqrt[3]{14 \cdot 14 \cdot 14}</math><br/><math>= \boxed{14}</math></p>   |
| <p>e. <math>\sqrt[3]{3375}</math></p> $\begin{array}{r} 5 \overline{) 3375} \\ \underline{675} \phantom{0} \\ 5 \overline{) 135} \\ \underline{27} \phantom{0} \\ 3 \overline{) 9} \\ \underline{3} \\ 0 \end{array}$ <p><math>\sqrt[3]{3375} = \sqrt[3]{15 \cdot 15 \cdot 15}</math><br/><math>= \boxed{15}</math></p>  | <p>f. <math>\sqrt[3]{4096}</math></p> $\begin{array}{r} 2 \overline{) 4096} \\ \underline{2048} \phantom{0} \\ 2 \overline{) 1024} \\ \underline{512} \phantom{0} \\ 2 \overline{) 256} \\ \underline{128} \phantom{0} \\ 2 \overline{) 64} \\ \underline{32} \phantom{0} \\ 2 \overline{) 16} \\ \underline{8} \phantom{0} \\ 2 \overline{) 4} \\ \underline{2} \\ 0 \end{array}$ <p><math>\sqrt[3]{4096} = \sqrt[3]{16 \cdot 16 \cdot 16}</math><br/><math>= \boxed{16}</math></p> |

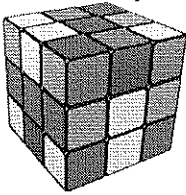
Name: \_\_\_\_\_

Block: \_\_\_\_\_

Date: \_\_\_\_\_

Calculators are allowed for the following questions.

3. How many small cubes are found in the 3x3 Rubik's cube pictured below?



$$3^3 = \boxed{27 \text{ small cubes}}$$

4. A rectangular swimming pool measures 8 feet wide, 16 feet long, and 4 feet deep. What are the dimensions of a cube shaped swimming pool that holds the same amount of water?

$$\begin{aligned} \text{Volume} &= l \times w \times h \\ &= 8 \times 16 \times 4 \\ &= 512 \end{aligned}$$

$$\begin{aligned} \text{Side length} &= \sqrt[3]{512} \\ &= \boxed{8 \text{ ft}} \end{aligned}$$

5. A cube shaped water reservoir holds 400 m<sup>3</sup> of water. How deep is it? Answer to the nearest tenth.

$$\text{Depth} = \sqrt[3]{400} = \boxed{7.4 \text{ m}}$$

$V = 400 \text{ m}^3$

6. If a cubical block contains 21 952 in<sup>3</sup>, how many square inches of paper will be required to cover the entire surface? (Remember, a cube has six sides)

$$\begin{aligned} \text{Side length} &= \sqrt[3]{21952} \\ &= 28 \text{ in} \end{aligned}$$

$$\begin{aligned} \text{Surface Area} &= 6(28 \times 28) \\ &= \boxed{4704 \text{ in}^2} \end{aligned}$$

$V = 21952 \text{ in}^3$

7. The entire surface area of a cubic block is 384 cm<sup>2</sup>. How many 1 centimetre cubes can be cut from the block?

$$\begin{aligned} \text{Area of one side} &= \frac{384}{6} \\ &= 64 \text{ cm}^2 \\ \text{Side length} &= \sqrt{64} \\ &= 8 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Number of } 1 \text{ cm} \times 1 \text{ cm} \times 1 \text{ cm} \\ \text{blocks} &= 8^3 \\ &= \boxed{512} \end{aligned}$$